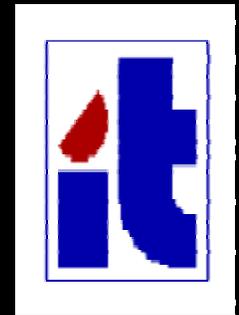


# Limitations imposed by cross - phase modulation in dense wavelength division multiplexing systems



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# *Motivation*

Optical networks with capacity of Tbit/s per fiber

Multi-channel (WDM) with very large number of channels

Limited EDFA's bandwidth

Narrow channel separation

Dense WDM

(channel separation of 50, 100, 200 GHz)

Inter-channel nonlinear effects (FWM, SRS, XPM) affect system performance

**XPM appears as one of the most detrimental effects over SMF and NZDSF**

# ***Cross - phase modulation (XPM)***

Power

of one optical wave propagating in an optical fiber changes  
the refractive index of the fiber which induces

phase shifts

in *other* co-propagating waves of different wavelengths

# *Outline*

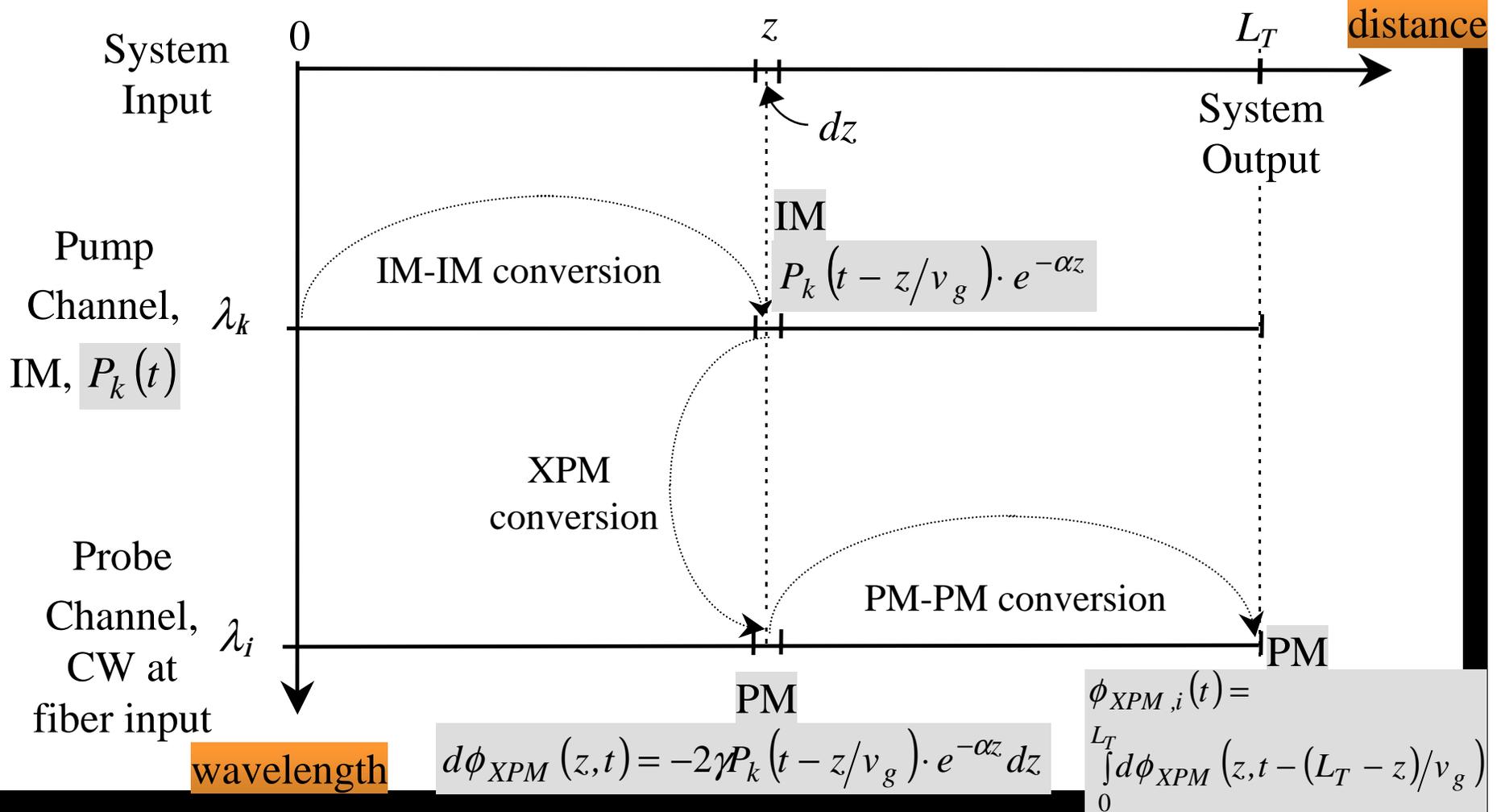


## XPM in optical fiber DWDM systems:

- How does it work?
- How does it limit the system performance?
- How can it be suppressed / reduced?

# *XPM-induced phase shift*

## *- dispersionless fiber -*



# *XPM-induced phase shift*

## *- dispersionless fiber -*

### ➤ One interfering channel

$$\phi_{XPM,i}(t) = -2\gamma P_k(t - L_T/v_{g,i}) \cdot L_{eff} \quad L_{eff} = [1 - e^{-\alpha L_T}] / \alpha$$

XPM-induced phase shift with same shape as power of interfering channel

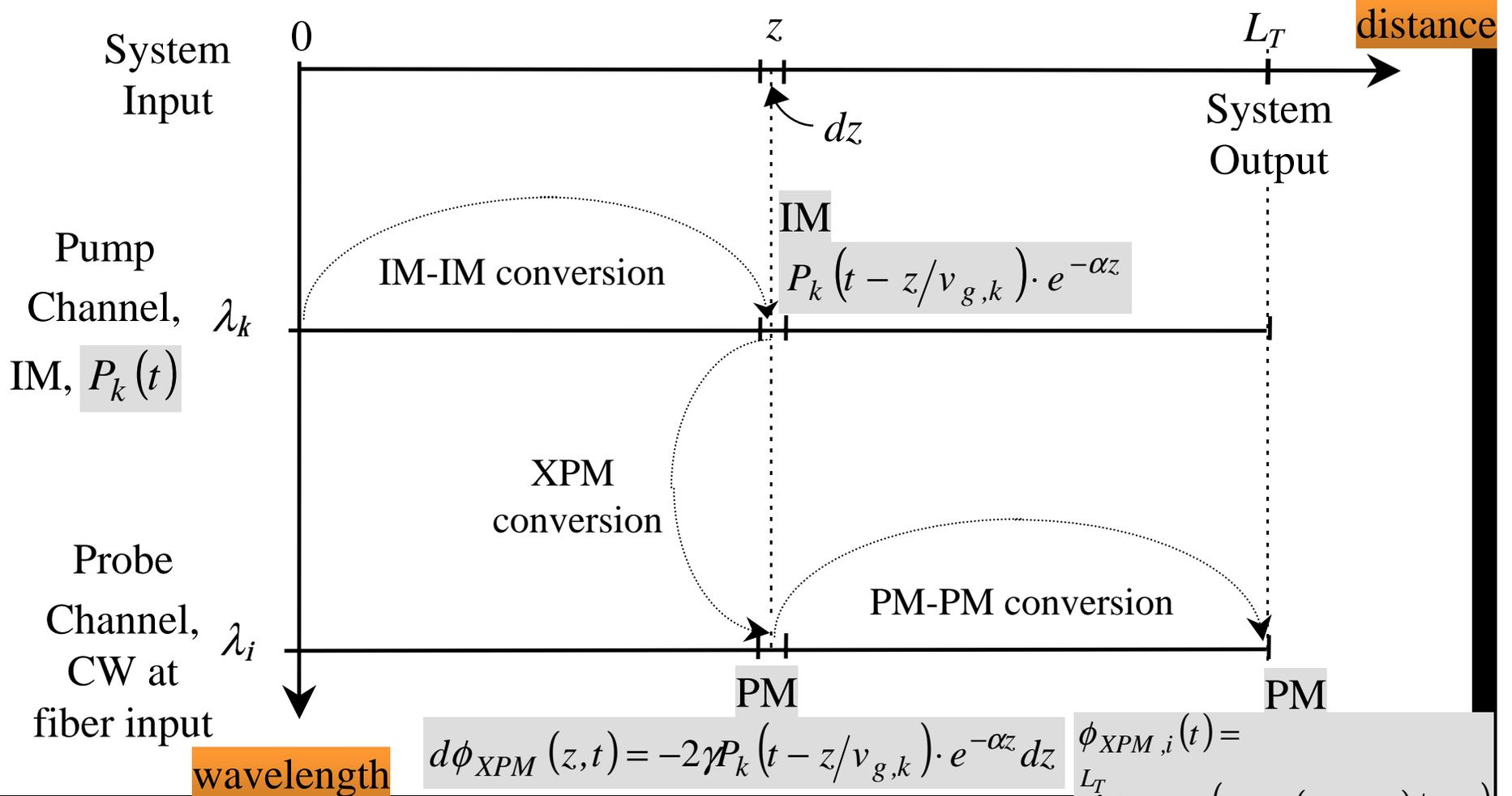
### ➤ $M$ interfering channels

$$\phi_{XPM,i}(t) = -2\gamma L_{eff} \sum_{k=1}^M P_k(t - L_T/v_{g,i})$$

Synchronized interfering channels  $\Rightarrow$  XPM-induced phase shifts add synchronously

# *XPM-induced phase shift*

## *- dispersive fiber -*



# *XPM-induced phase shift*

## *- dispersive fiber -*

### ➤ One interfering channel

$$\phi_{XPM,i}(t) = -2\gamma \int_0^{L_T} P_k(t - L_T/v_{g,i} - d_{k,i}z) \cdot e^{-\alpha z} dz \quad d_{k,i} = v_{g,k}^{-1} - v_{g,i}^{-1}$$

Walk-off parameter

(normalized delay propagation difference)

### ➤ $M$ interfering channels

$$\phi_{XPM,i}(t) = -2\gamma \sum_{k=1}^M \int_0^{L_T} P_k(t - L_T/v_{g,i} - d_{k,i}z) \cdot e^{-\alpha z} dz$$

$$d_{k,i} = \int_{\lambda_i}^{\lambda_k} D(\lambda) d\lambda \approx D(\lambda_i) \cdot (\lambda_k - \lambda_i)$$

XPM-induced phase shift spread over time (shape different from the power of interfering channel)

XPM-induced phase shifts do not add synchronously

**Reduction of XPM efficiency**

# *XPM in IM-DD systems*

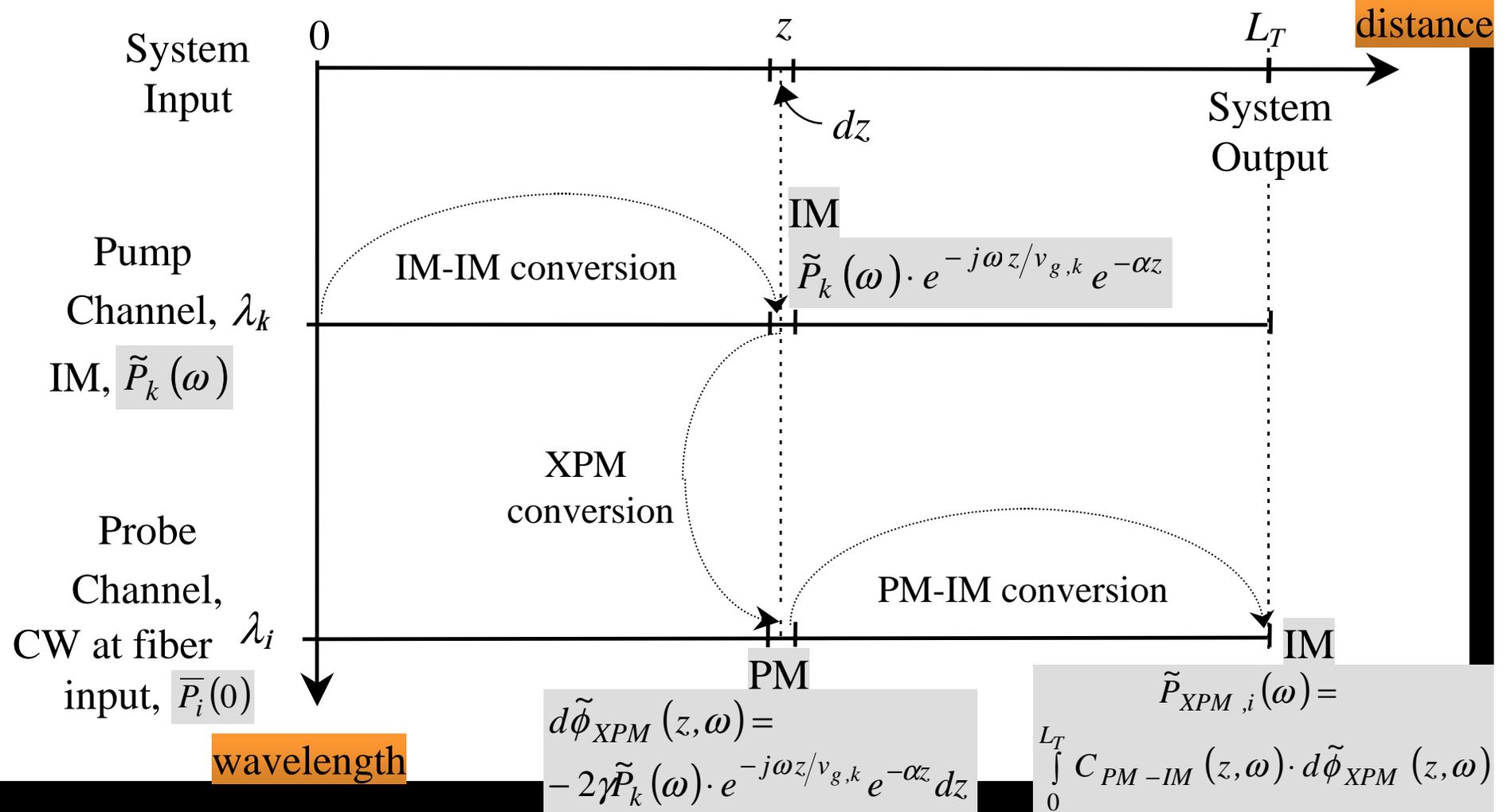
- Current receivers based on direct detection (DD) are insensitive to phase variations

but ...

- Fiber dispersion converts pattern-dependent XPM-induced phase shifts to power fluctuations
  - ▶ XPM manifests in waveform distortion leading to eye diagram deformation

**Phase shifts (frequency chirping) + GVD  $\Rightarrow$  intensity fluctuations**

# Physical explanation of XPM effect in IM-DD systems



# *XPM-induced IM* *caused by group velocity dispersion*

## ➤ One interfering channel

$$\tilde{P}_{XPM,i}(\omega) = \int_0^{L_T} \underbrace{\bar{P}_i(0)e^{-\alpha z}}_{\text{Average probe power at co-ordinate } z} \cdot \underbrace{e^{-j\omega(L_T-z)/v_{g,i}}}_{\text{Propagation delay in probe channel}} \cdot \underbrace{e^{-\alpha(L_T-z)}}_{\text{Fiber loss due to propagation in probe channel}} \sin\left(\omega^2 \frac{D(\lambda_i)\lambda_i^2}{4\pi c}\right) \cdot d\tilde{\phi}_{XPM}(z, \omega)$$

Small signal PM-IM conversion

$$\tilde{P}_{XPM,i}(\omega) = -2\gamma\bar{P}_i(0)\tilde{P}_k(\omega)e^{-\alpha L_T} \cdot e^{-j\omega L_T/v_{g,i}} \int_0^{L_T} e^{-j\omega z d_{k,i}} e^{-\alpha z} \cdot \sin\left(\omega^2 \frac{D(\lambda_i)\lambda_i^2}{4\pi c}\right) dz$$

$$\tilde{P}_{XPM,i}(\omega) = H_{i,k}(\omega) \cdot \tilde{P}_k(\omega)$$

$$P_{XPM,i}(t) = F^{-1}[\tilde{P}_{XPM,i}(\omega)]$$

## ➤ M interfering channels

$$\tilde{P}_{XPM,i}(\omega) = \sum_{k=1}^M H_{i,k}(\omega) \cdot \tilde{P}_k(\omega)$$

## *Features of XPM-induced IM*

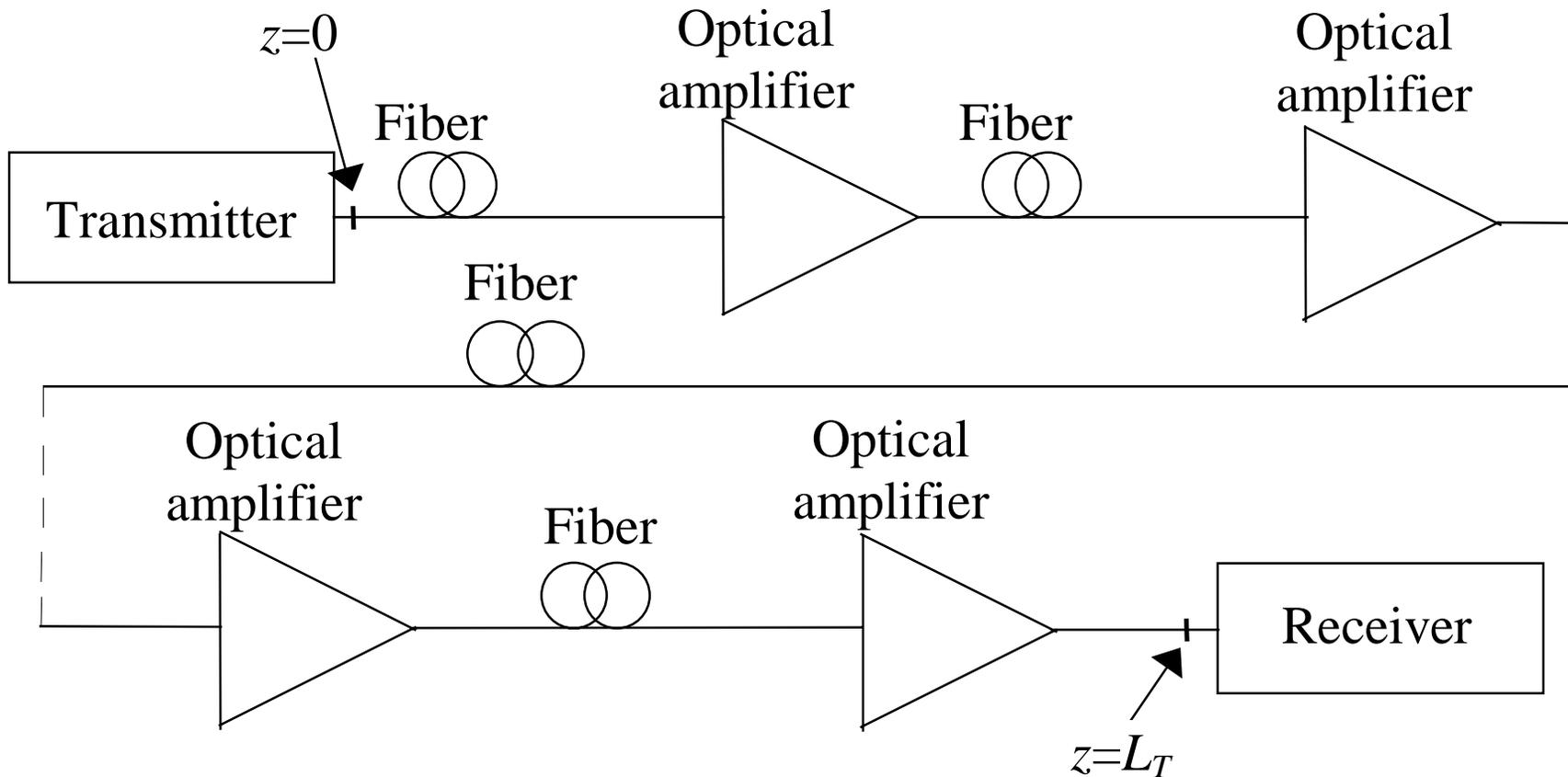
- Depends on bit in probe channel
  - Vanishes for null power in probe channel
- Depends on average power, bit and pulse shape in interfering channel
  - Vanishes for constant power in interfering channel

Signal dependence leads to stochastic XPM-induced intensity distortions

When an edge in the interfering channel overlaps with a signal pulse, XPM-induced chirp is introduced

- The main contribution to XPM effect comes from adjacent channels
- XPM effect is maximized when pulses in neighboring channels are time-aligned in the front part of the fiber

# *Multiple span fiber link*



- Several configurations can be investigated through appropriate choice of optical amplifiers' gain and fiber segment properties.

## *Normalized XPM-induced IM index*

- Normalized magnitude of IM response induced by XPM in the probe channel  $i$

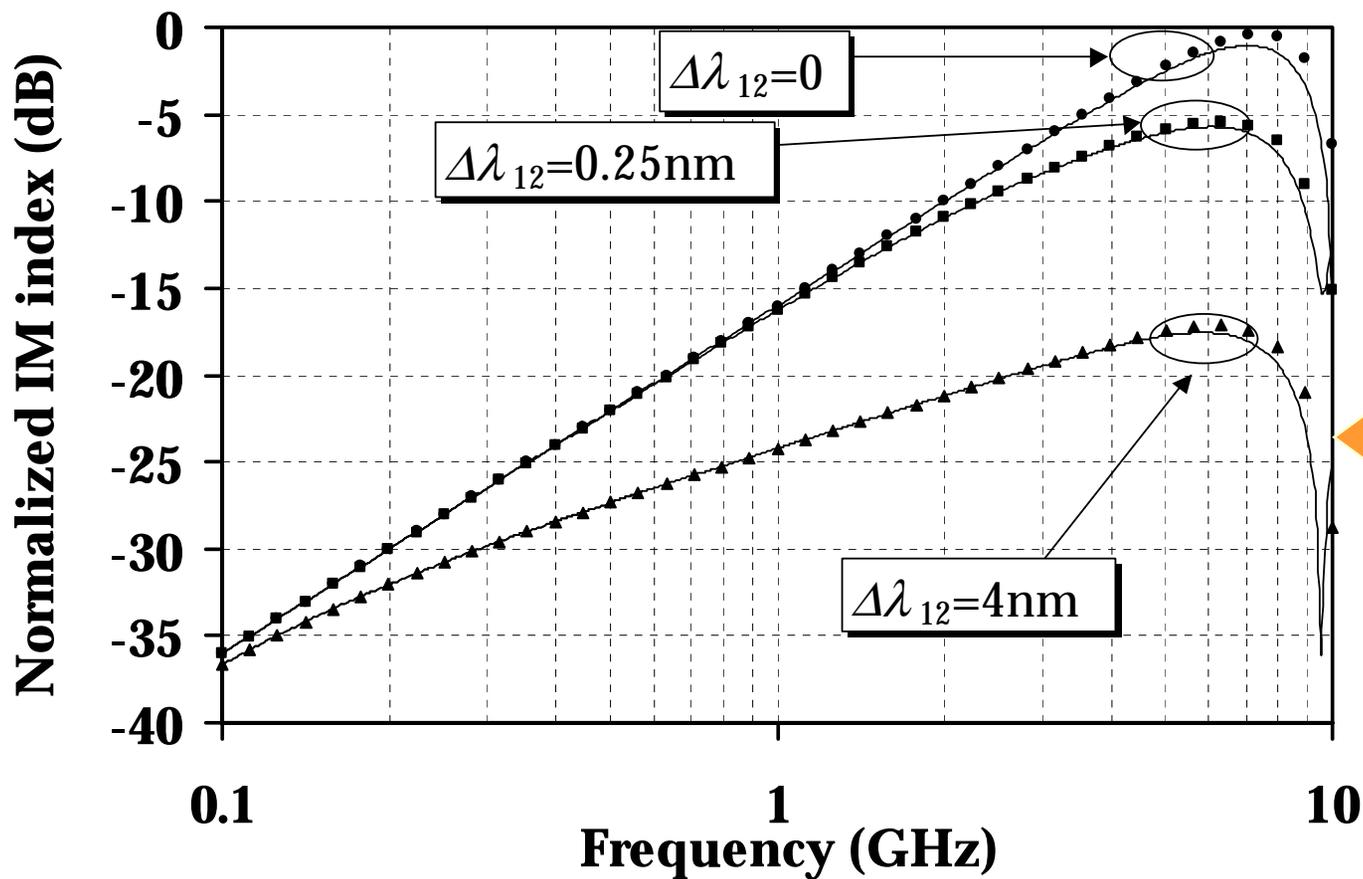
$$m_{IM,i}^{XPM} = \left| \tilde{P}_{XPM,i}(\omega) / \left( \tilde{P}_k(\omega) \cdot g_i^{net}(L_T) \right) \right|$$

➔ *net* power gain for the  $i$ -th channel from the transmitter up to the receiver

$$g_i^{net}(L_T) = \prod_{n=1}^N e^{-\alpha^{(n)} L^{(n)}} g_i^{(n)}$$

# Normalized XPM-induced IM index

Single span of 80 km of SMF, 2 channels



$$\Delta\lambda_{12} = \lambda_1 - \lambda_2$$

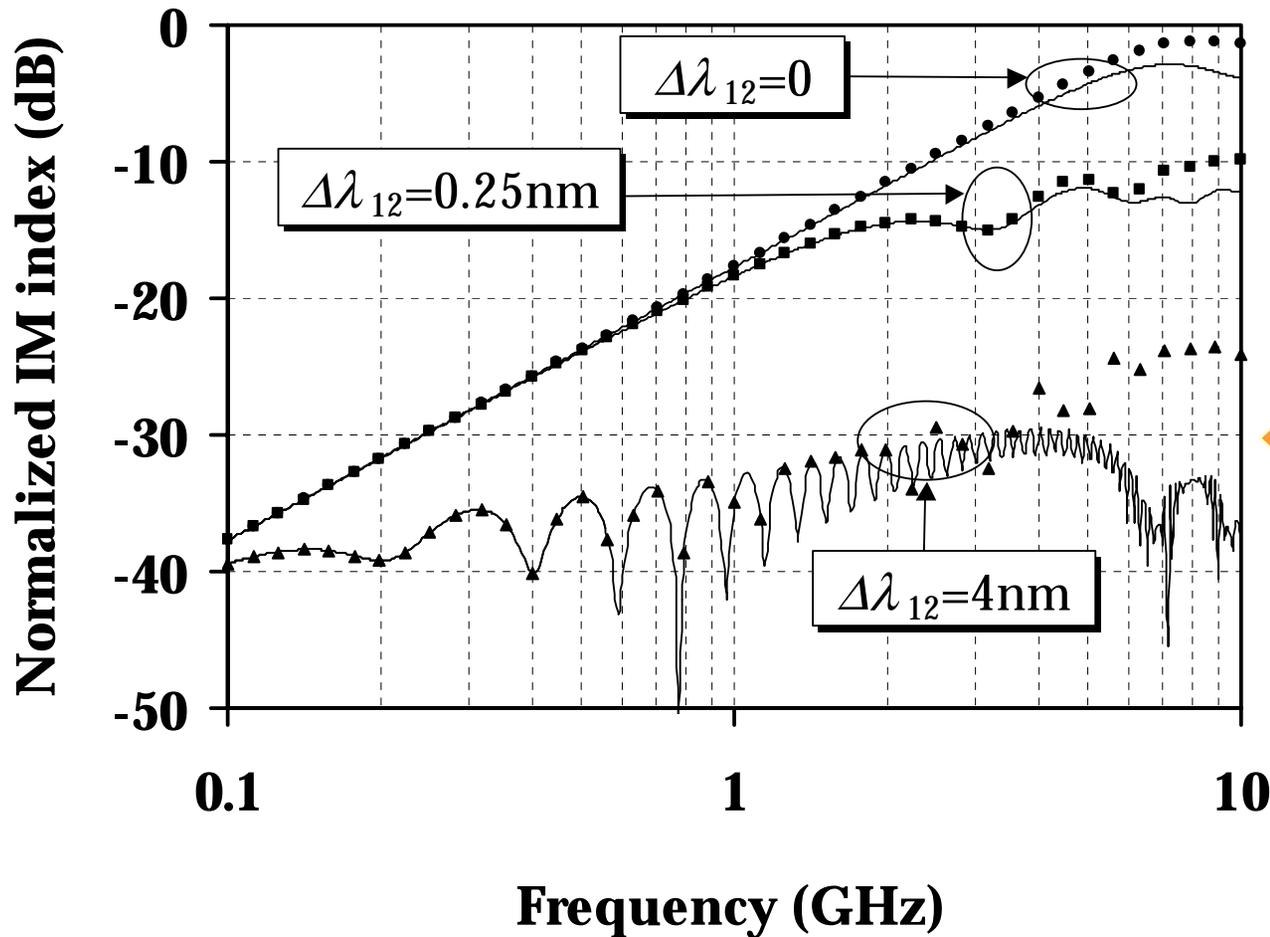
Average power /  
channel at fiber  
input = 10 dBm

Simple high-pass  
characteristic

PM-IM  
conversion  
caused by GVD

# Normalized XPM-induced IM index

Four spans of 80 km of SMF dispersion compensated  
(after each SMF span) by DCF, 2 channels

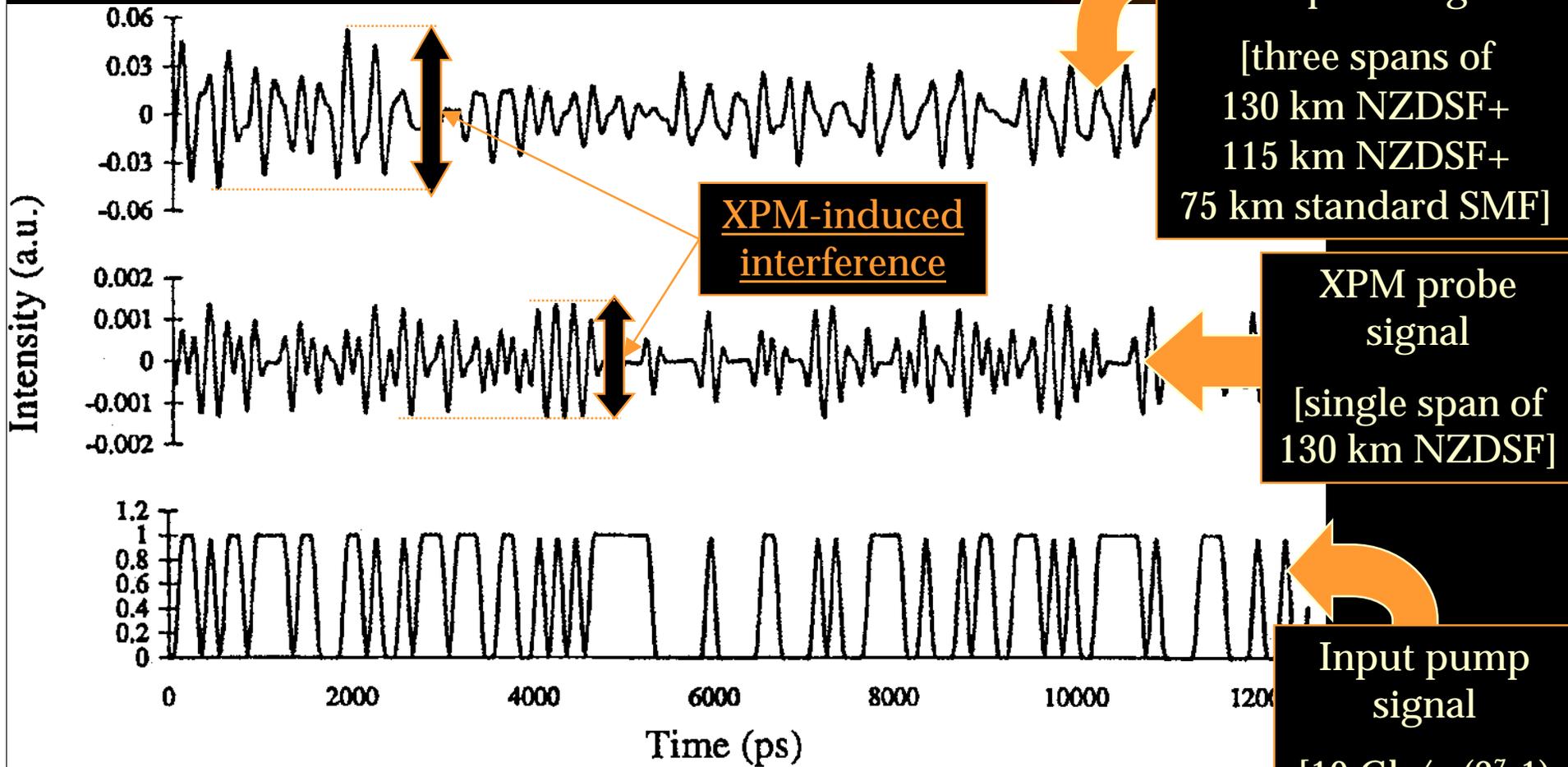


Average power /  
channel at fiber  
input = 7 dBm

Characteristic with  
various dips  
(notches) whose  
location depends  
on channel  
separation and  
span length

# XPM time domain waveforms

2 channels, 0.8 nm of channel separation



From Hui *et al.*, JLT, pp. 1018-1026, June 1999.

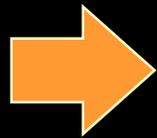
2001.09.07

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# *Measure for the extent of the XPM-induced signal distortion*

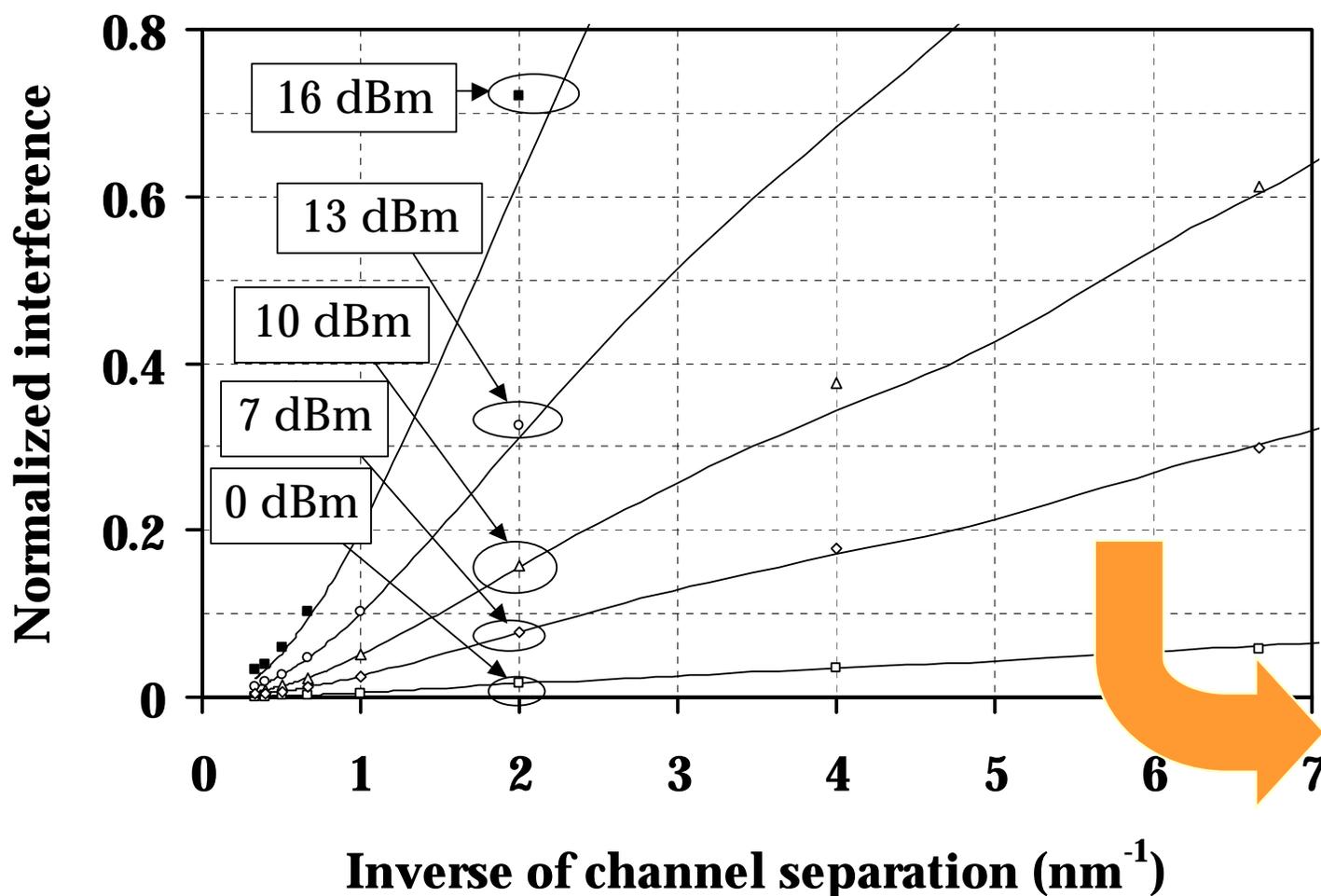
## Normalized interference induced by XPM



ratio of the  
difference between maximum and minimum value of the  
intensity of the probe channel and  
the average value of the intensity in the probe channel

# Normalized interference induced by XPM

Single span of 80 km of SMF, 3 channels

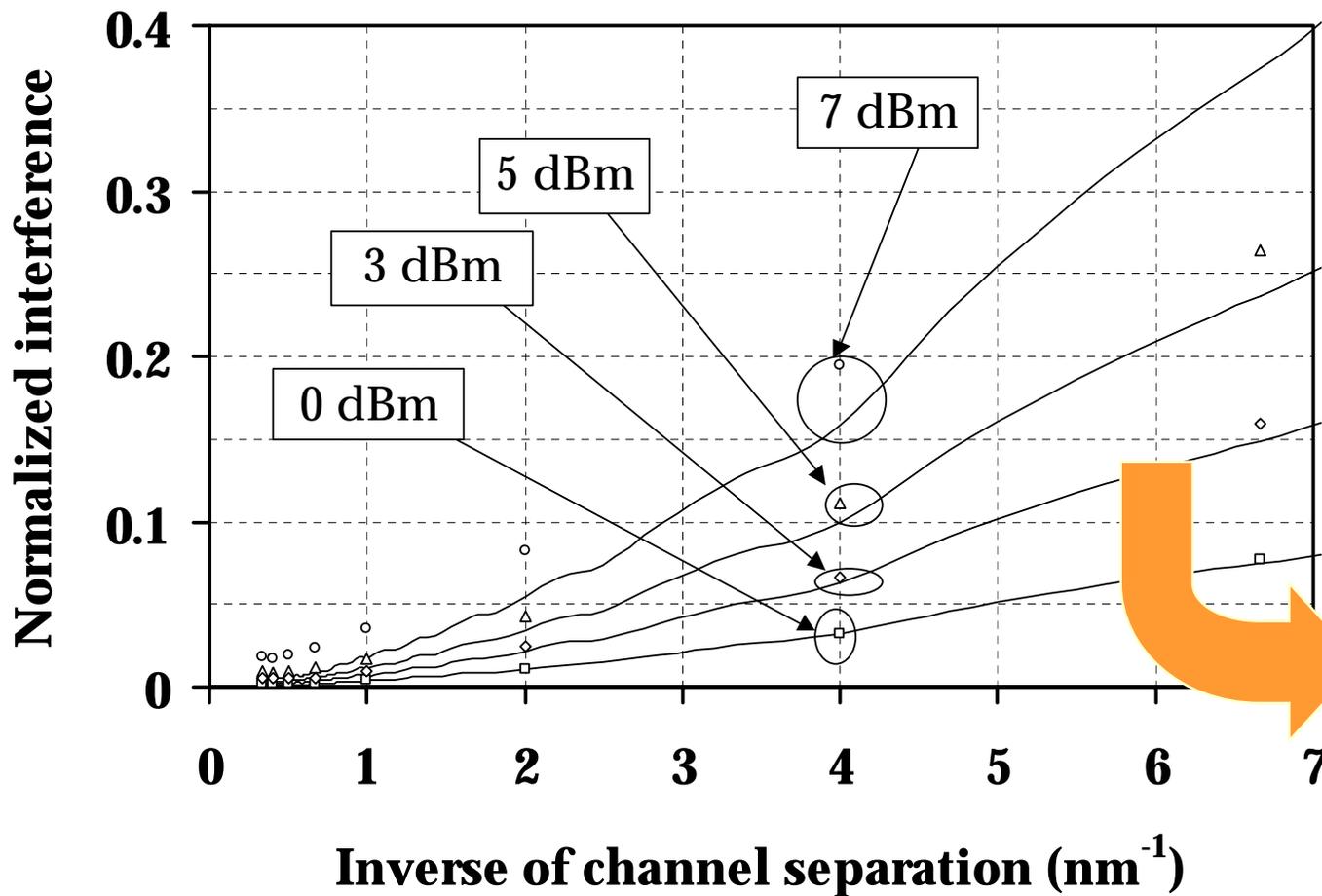


Pump channel externally (chirpless) modulated with a  $2^7$  bit sequence at 5 Gb/s

XPM interference increases linearly with interfering signal power and inversely with channel separation

# Normalized interference induced by XPM

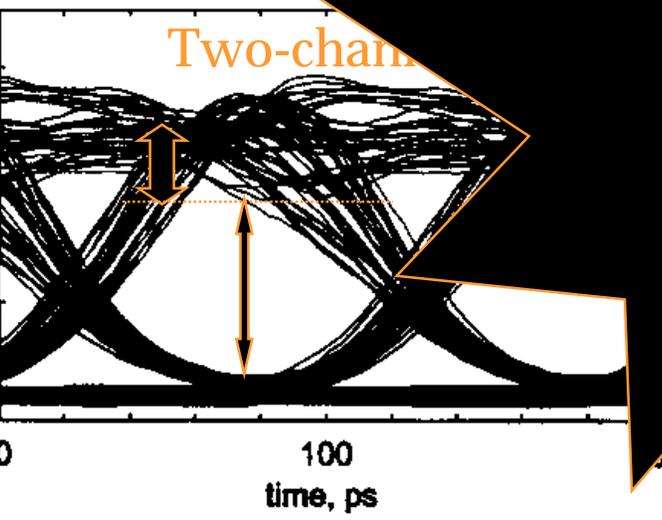
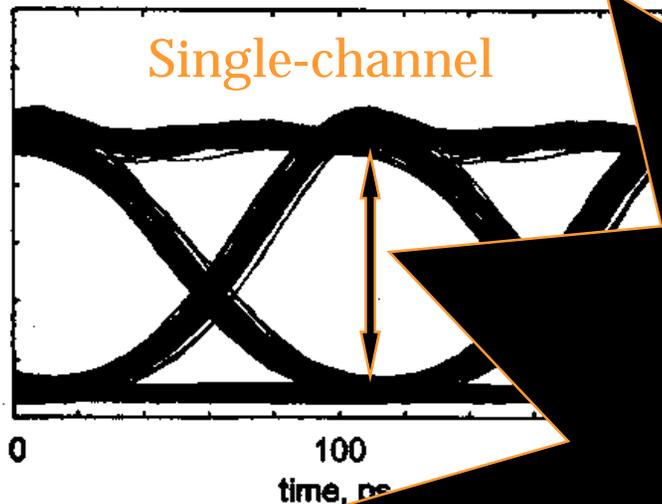
Four spans of 80 km of SMF dispersion compensated  
(after each SMF span) by DCF, 2 channels



Pump channel externally (chirpless) modulated with a  $2^7$  bit sequence at 5 Gb/s

XPM interference increases linearly with interfering signal power and inversely with channel separation

# Estimating the XPM-induced system penalty from CW probe results



*An approach has been presented to estimate the reduction in Q factor due to XPM using XPM-induced IM distortion of a CW probe*

modulation of CW probe by interfering channel

80 km of NZDSF, 10 Gb/s, 10 dBm,  $\Delta\lambda=0.8\text{nm}$

Change of bit alignment: look at perturbed CW trace at different times

# Timing jitter induced by XPM

Frequency chirping (due to XPM-induced phase shift) + propagation through dispersive fiber (slightly different group velocity)  $\rightarrow$  pulse timing jitter

Worst-case timing jitter:  
jitter caused by the first interfering edge at the fiber input

The nonlinear interaction response occurs only in the first

$$L_{eff} \approx L_{wo} = \epsilon T / (D)$$

Ass

**It can be the main impairment for high bit rates approaching 40 Gbit/s**

Collision:  
interfering pulse has part way through the signal

Frequency chirping:

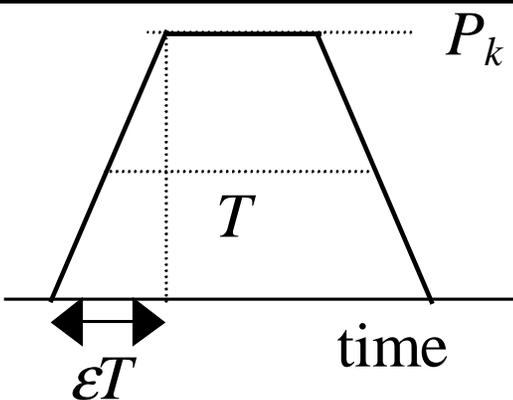
$$\approx -2\gamma P_k / (2\pi\epsilon T) \cdot L_{wo}$$

Timing jitter:

$$|\delta t| = L \cdot \delta f_{XPM} \cdot \lambda^2 / c = 2\gamma P_k L / (2\pi\Delta f)$$

Jitter value:

- $\rightarrow$  independent of dispersion parameter
- $\rightarrow$  independent of bit rate



# Timing jitter induced by XPM



**By using positive prechirping and normal dispersion fibers, the system performance is improved**

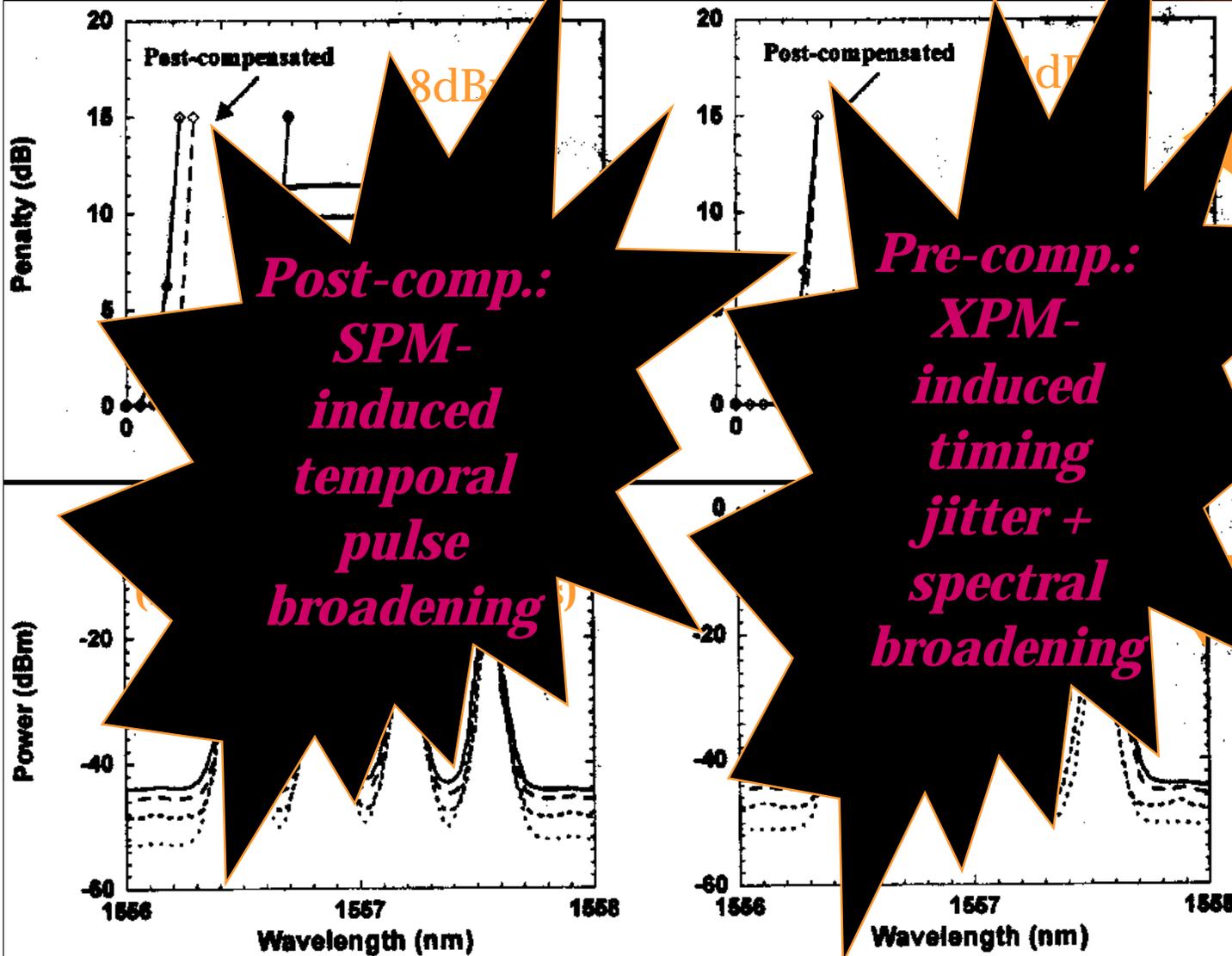
$\alpha_c = 0.7, D = -2 \text{ ps/nm/km}$

4 NRZ channels at 40 Gbit/s  
200 GHz of channel separation  
km exactly post-DC, to  
the receiving terminal

$2 \text{ ps/nm/km}, D_{tot} = 70 \text{ ps/nm}$

$2^7 - 1$  PRBS is shifted by a quarter period from the sequence of the neighboring channel

# Spectral broadening induced by XPM



*Post-comp.:  
SPM-  
induced  
temporal  
pulse  
broadening*

*Pre-comp.:  
XPM-  
induced  
timing  
jitter +  
spectral  
broadening*

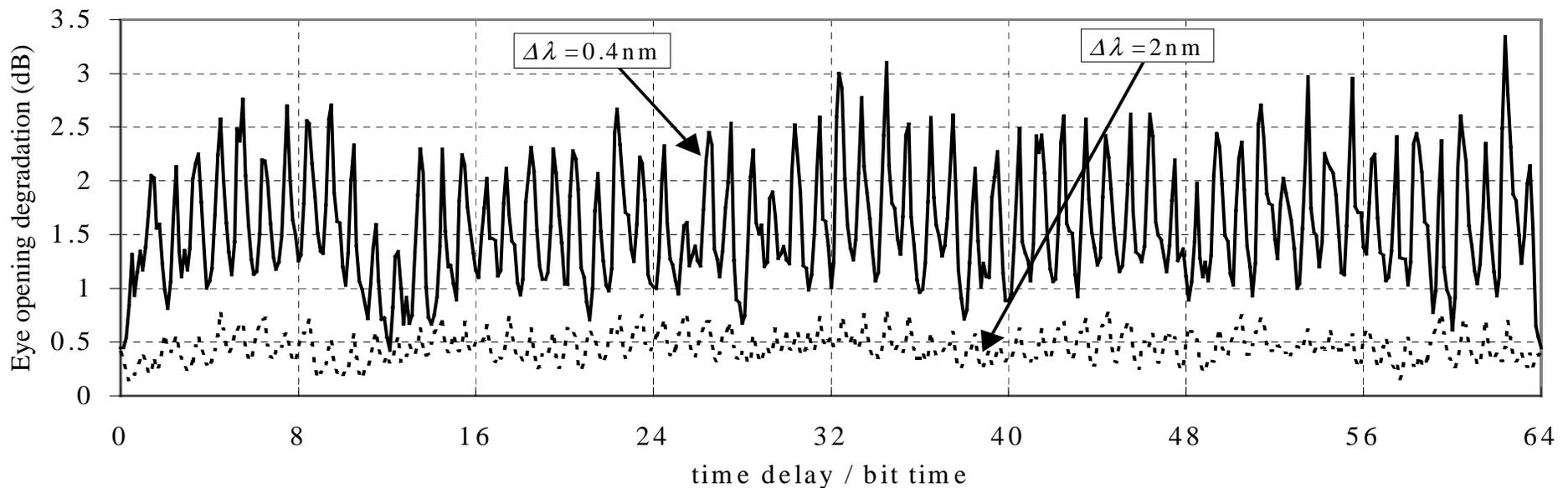
Four channel, 10 Gb/s, spans of 40 km of SMF compensated exactly by DCF

Spectral broadening leads to coherent crosstalk between spectral components of neighboring channels in DWDM system

This effect is enhanced in NZDSF

# *XPM dependence on relative delay between channels*

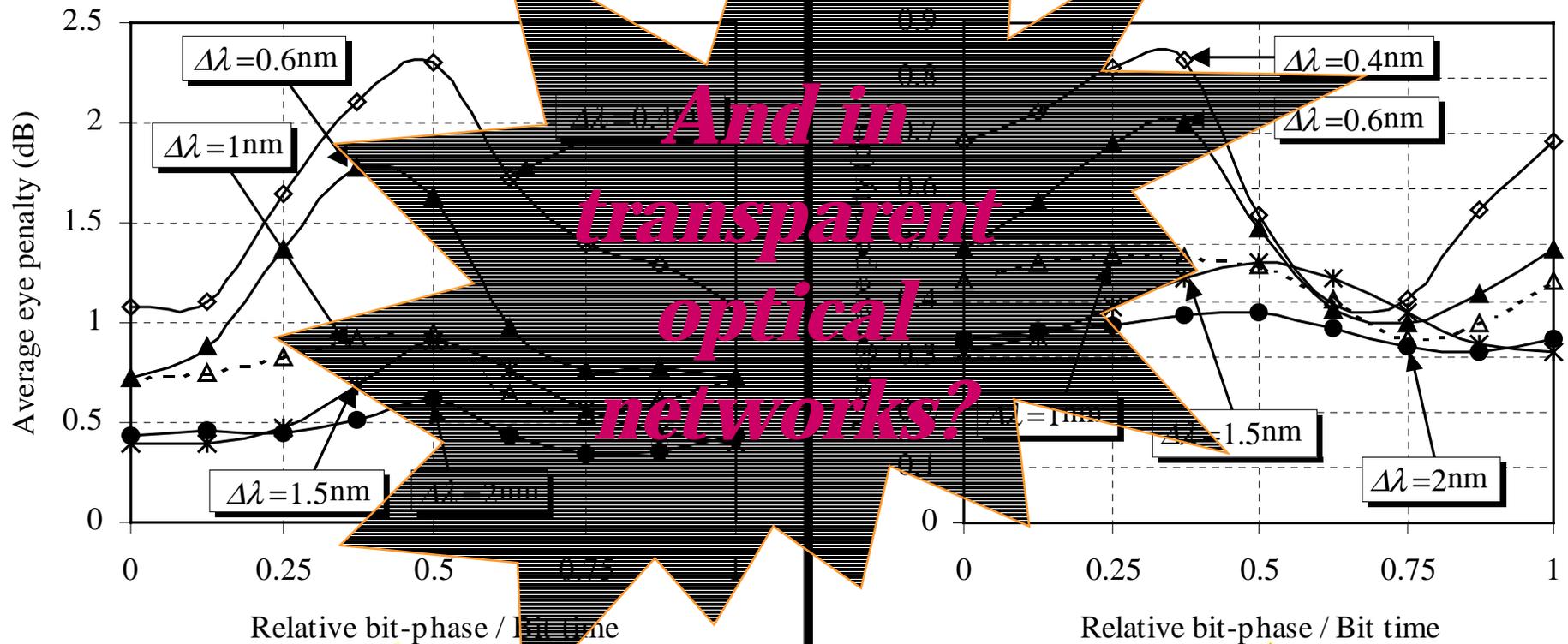
**System length = 360km of SMF, amplifier span = 120km, peak power = 30mW, two-channel at 2.5 Gb/s**



8 time delays per bit are examined and sequences of  $N_b=64$  bits are used in the simulation  $\Rightarrow$  512 simulations corresponding to 512 different time delays are performed for each set of system parameters.

# *XPM dependence on relative bit-phase between channels (point-to-point links)*

System length = 360km of SMF, amplifier span = 20km, 2 channels at 2.5 Gb/s



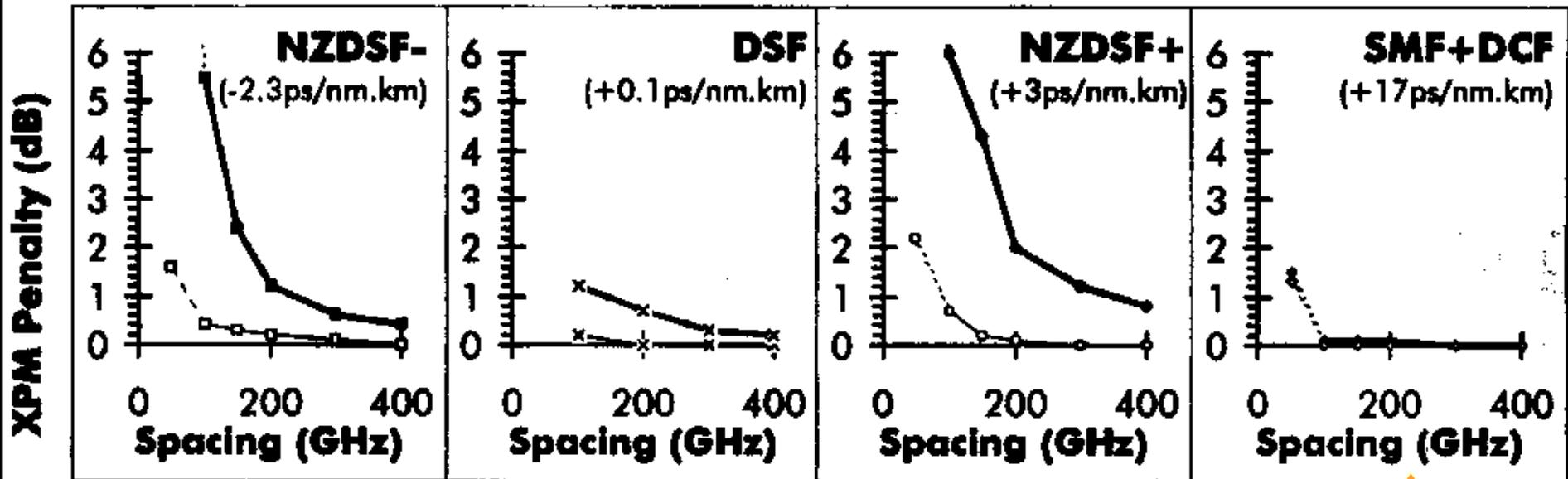
Peak power = 30mW

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Peak power = 10mW

# XPM dependence on type of fiber infrastructure

Two identical 100 km long fiber spans, 10 Gb/s



- Thick lines: worst case
- Thin lines: best case
- Worst and best cases obtained as the relative signal-pump polarization and delay are adjusted

Residual dispersion of  $-320$  ps/nm

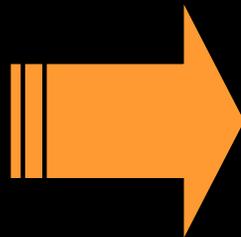
From Bigo *et al.*, IEEE PTL, pp. 605-607, May 1999.

# *Suppression of XPM*

- By using source polarisation optimization
- By controlling appropriately the prechirping at transmitter
- By controlling the relative time delays of adjacent channels at the transmitter

only applicable to point-to-point links

➤ By appropriate compensation of the fiber dispersion (does not remove the XPM-induced chirp!!!)

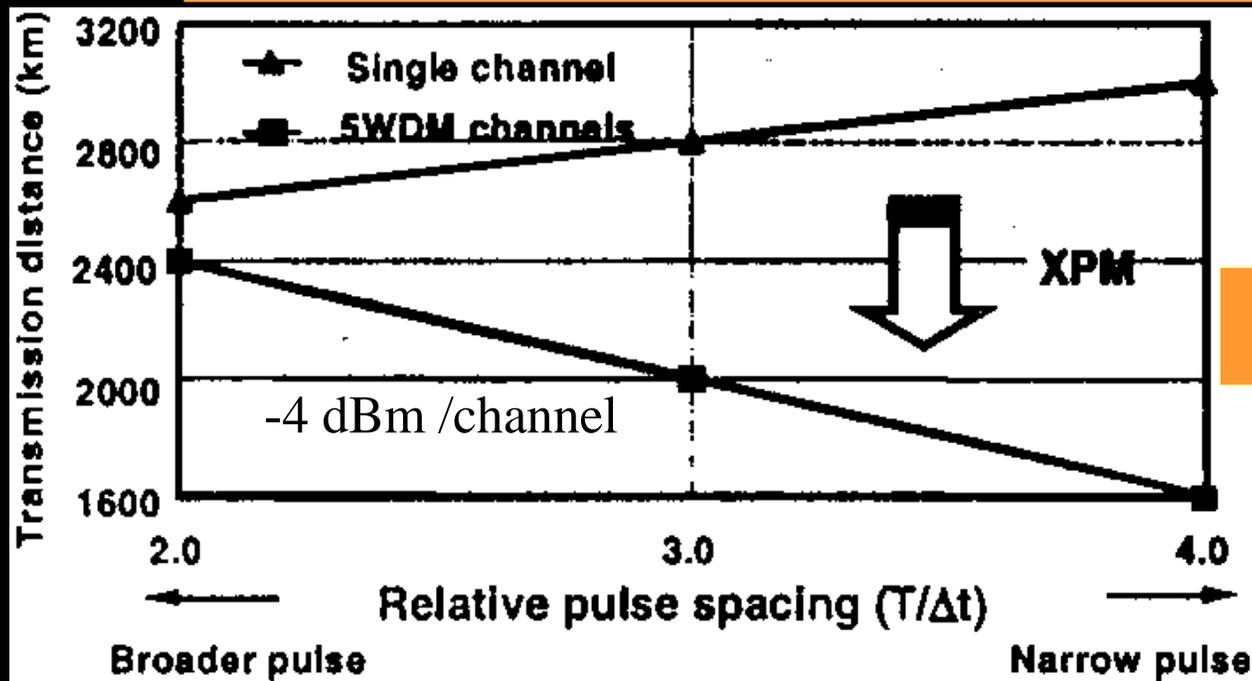


Inconsistent with full GVD compensation at each span (which requires also in-line dispersion slope compensation) ...

but causes realignment of the relative time delay between channels

# Suppression of XPM by pulse-width optimisation

20 Gbit/s/ch, 5 channels, channel spacing of 0.4 nm,  
20 km SMF + 20 km RDF per span



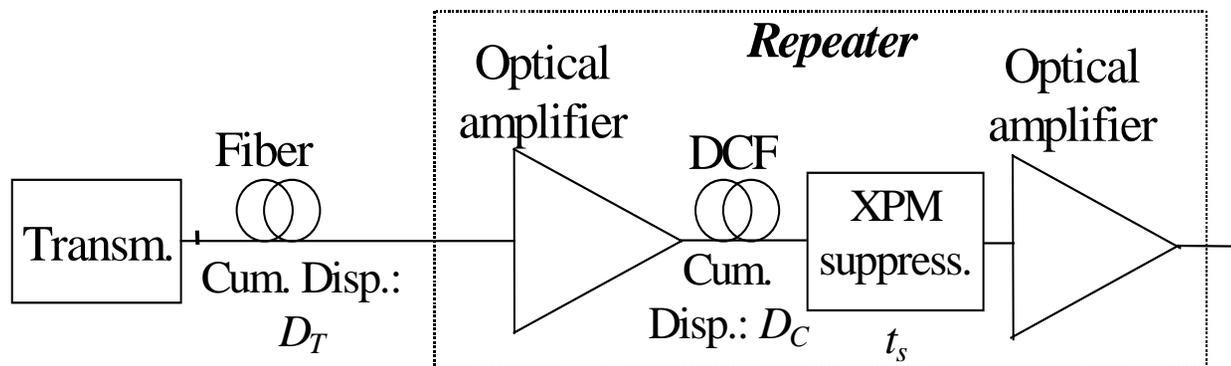
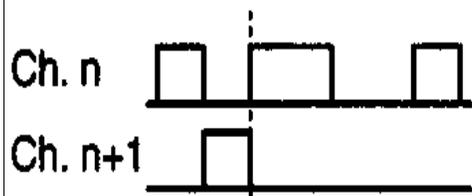
Single-channel:  
decrease of pulse width

Multi-channel:  
increase of pulse width

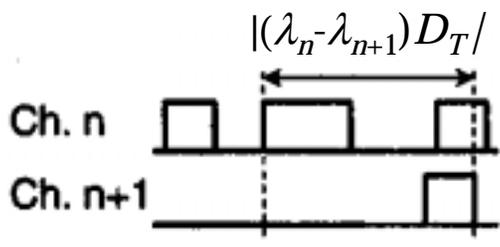
To suppress XPM in DWDM systems, wider pulses are desirable because of their less peak power (duty-cycle of 50% is suitable)

# Suppression of XPM by controlling the timing delays at each span

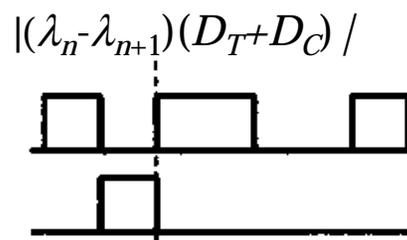
(a) First fiber input



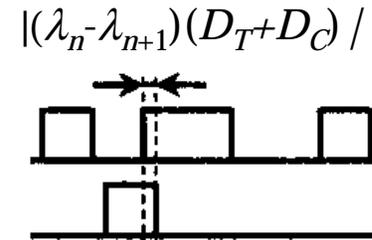
(b) No compensation



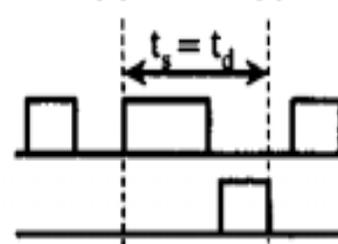
(c) Full compensation



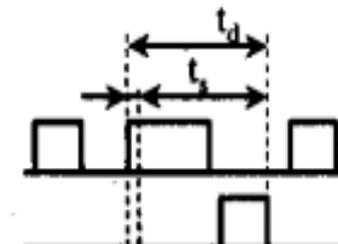
(d) Partial compensation



(e) Like (c) with suppressor



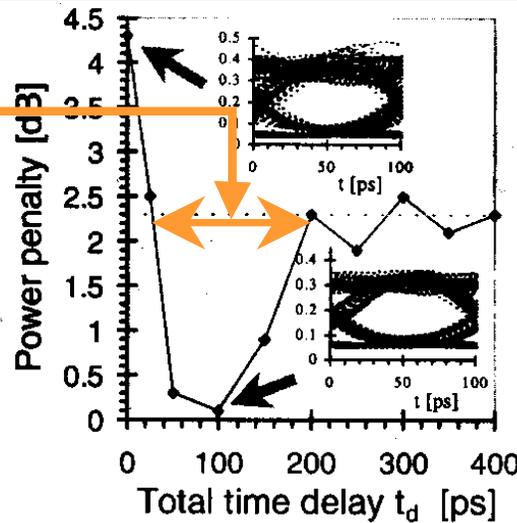
(f) Like (d) with suppressor



**Key idea:** to force the destructive addition between the contributions of the different spans to the overall XPM-induced IM by introducing adequate time delays between adjacent channels at the repeaters

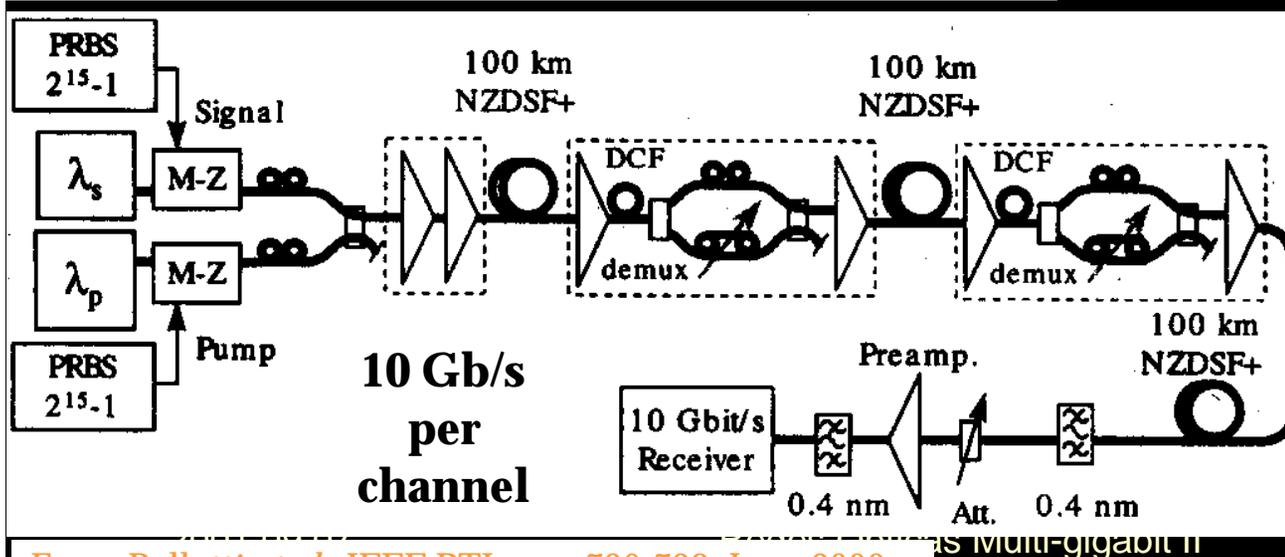
# Suppression of XPM by controlling the timing delays ... (cont.)

The delays need not to be set with very high precision: relaxed design of XPM suppressor



The XPM suppressor can be based on

- Integratable delay lines between demux/mux stages
- Series of narrow-band fiber Bragg gratings written at specific locations



- Avoid the need of management of GVD and dispersion slope to suppress the XPM effect

- Suppress the BER floor due to XPM

## *Conclusions*

- The main features of XPM have been identified and discussed.
- The ways, by which XPM limits the IM/DD DWDM system performance, have been highlighted.
- Several strategies for suppressing or reducing the degradation caused by XPM in DWDM systems have been presented and their main advantages and drawbacks have been discussed.
- **XPM can be the most detrimental effect in DWDM systems over SMF and NZDSF at both low and high bit rates.**



***Thank you  
for  
your attention !!!***