

Dispersion and self-phase modulation compensation in multi-gigabit systems

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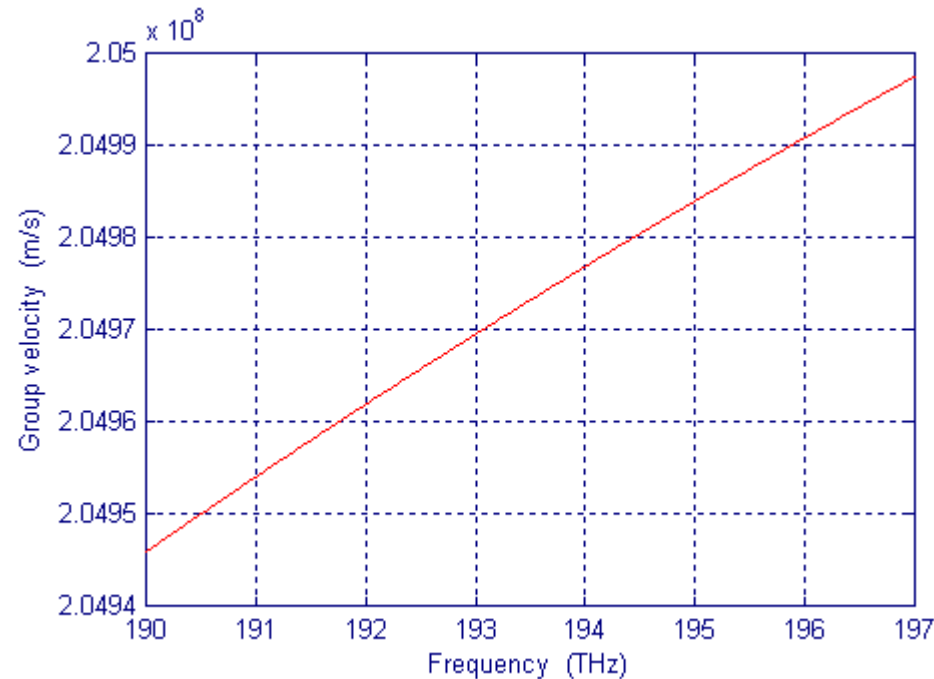


Limitations to the system performance

- Attenuation
- Dispersion
- Non-linear effects:
 - Self-phase modulation:
 - Pulse
 - Interaction between pulses
 - Cross-phase modulation
 - Four wave mixing
 - Stimulated Raman scattering
 - Stimulated Brillouin scattering
- Optical amplifiers ASE noise



Chromatic Dispersion



$$L_a = 100 \text{ km} \quad \Delta f = 50 \text{ GHz}$$

$$D = 17 \text{ ps/nm/km}$$

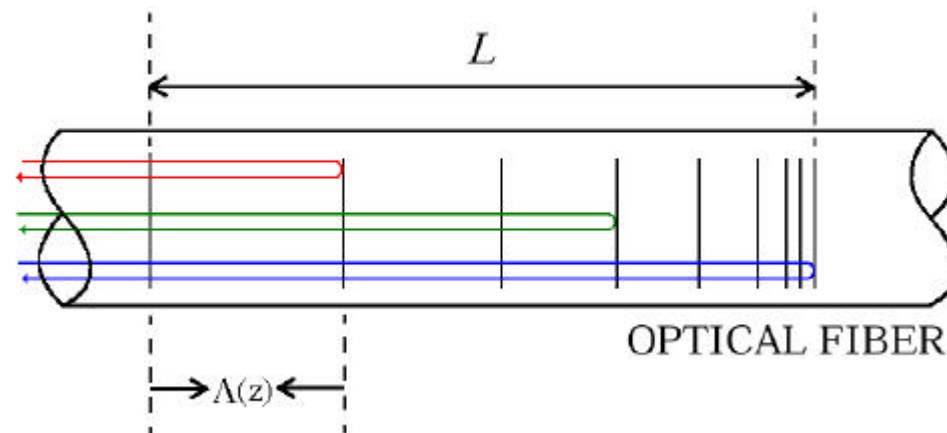
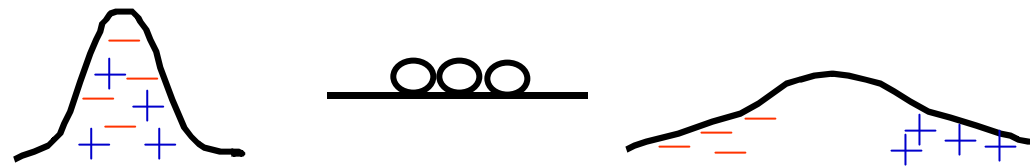


$$\text{TIME DELAY} = 680 \text{ ps}$$

$$\text{SPACE DELAY} = 14 \text{ cm}$$



Dispersion compensation



Limitations due to the dispersion

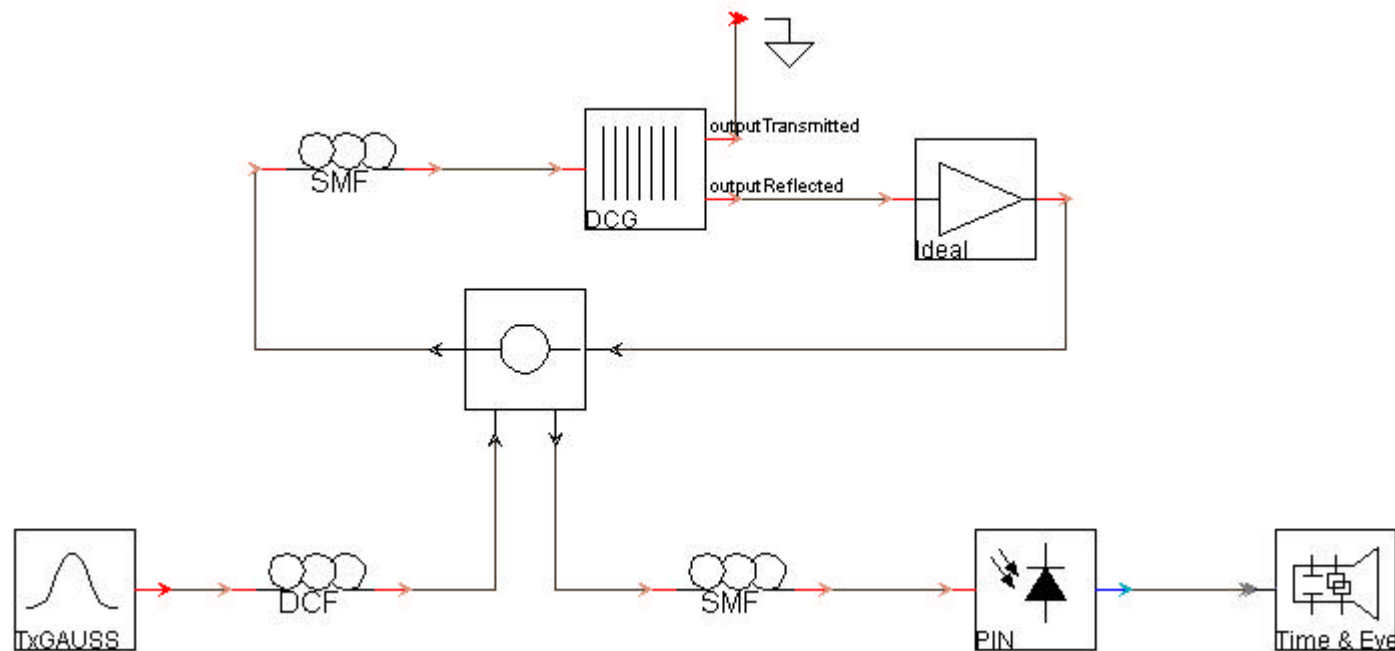
- Return to zero coding
- Pulse FWHM broadens to the extent of one bit slot time
- Standard fiber

Bit rate (Gbit/s)	Bit period (ps)	FWHM (ps)	Disp. length (km)
2.5	400	80	565
10	100	20	35
40	25	5	2.2
100	10	2	0.35



Prechirp+poscompensation+poschirp

■ SYSTEM LAYOUT ON THE PTDS SIMULATION TOOL:



■ A 100 ps^2 pre-chirp is attained with a negative dispersion fiber.



Prechirp+poscompensation+poschirp

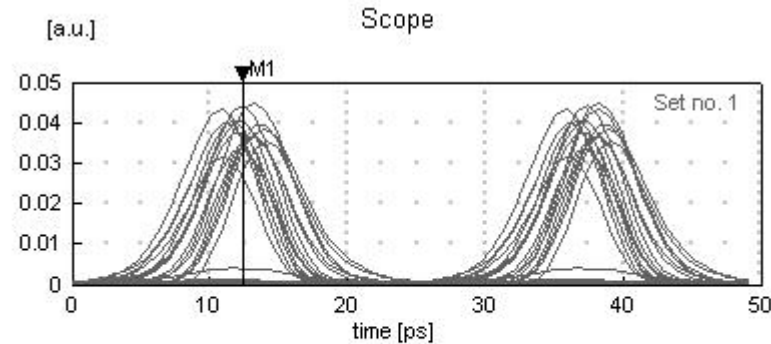
■ SYSTEM PARAMETERS:

Bit Rate	40 Gbit/s
Full width half maximum	5 ps
Wavelength	1553 nm
Spontaneous emission factor	2
Fiber attenuation	0.25 dB/km
Dispersion coefficient	- 20 ps ² /km
Gaussian pulse peak power	50 mw
Non-linear coefficient	1.3 W/km
Amplifiers spacing	100 km



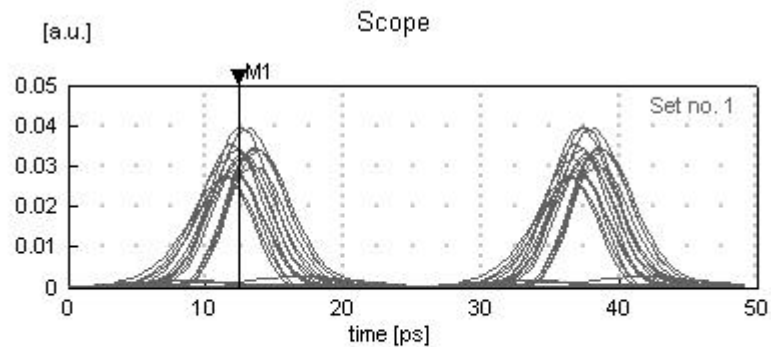
SIMULATION RESULTS FOR A MAXIMUM BER OF 10^{-9}

- Without pre-chirp a total distance of 1200 km was achieved:



time [ps]	M1: 12.5	M2: -	D2-1: -
[a.u.]	-	M2: -	D2-1: -
Q = 6.49	BER = 3.35e-011	EyeOpening = -34.3 dB	

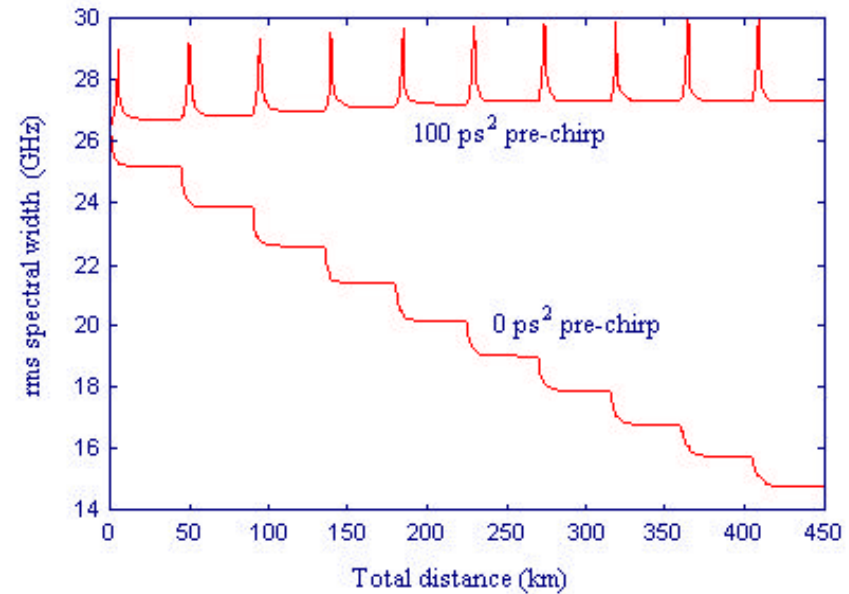
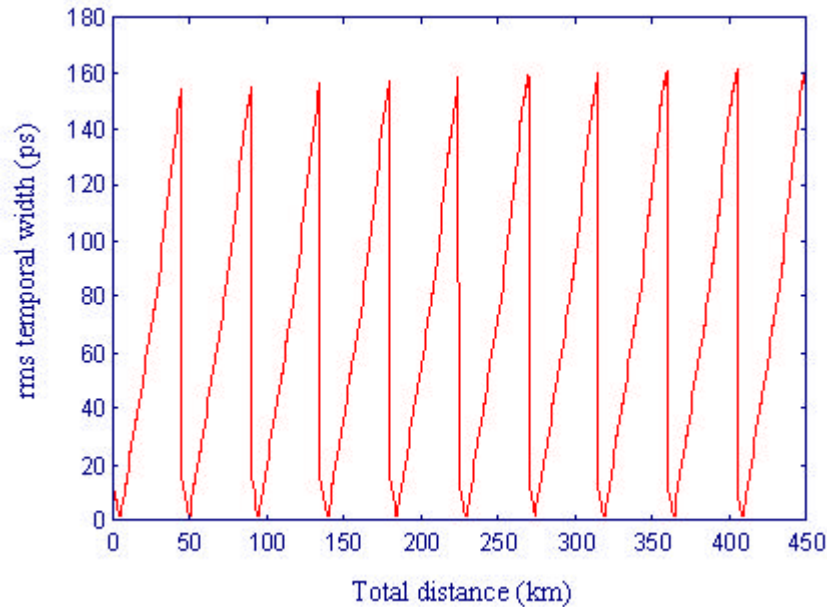
- With pre-chirp a total distance of 1800 km was achieved:



time [ps]	M1: 12.5	M2: -	D2-1: -
[a.u.]	-	M2: -	D2-1: -
Q = 6.11	BER = 3.17e-010	EyeOpening = -36 dB	



Self-phase modulation compensation



■ Pre-chirp computation [Zitelli99]:

$$\frac{\exp\left(\alpha \left| \frac{T_0^2 C_{pr}}{\beta_2} \right| \right) - 1}{\alpha \left| \frac{T_0^2 C_{pr}}{\beta_2} \right|} \frac{C_{pr}^2}{\left(1 + \frac{C_{pr}^2}{4}\right)^{\frac{3}{2}}} = 0.7698$$



ASE noise jitter

■ ASSUMPTIONS:

- Poscompensation of first order dispersion.
- No second order dispersion $\beta_3 = 0$.
- No non-linear pulse interaction.
- One channel at 40 Gbit/s.

■ HYPOTHESES:

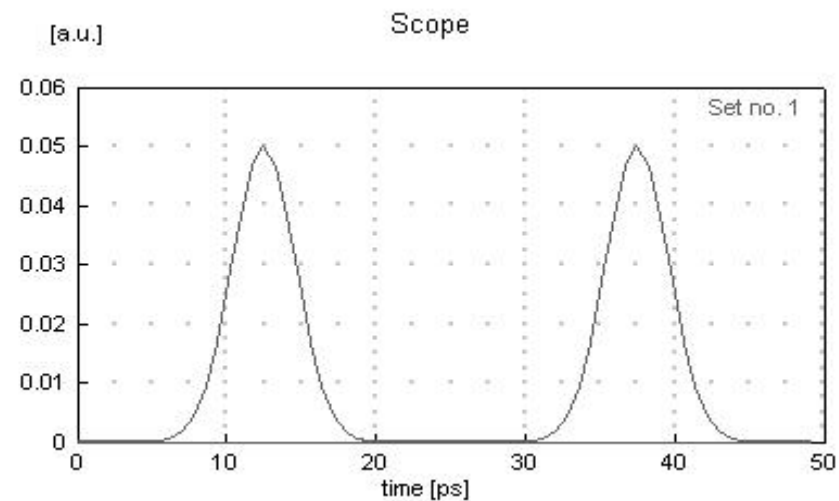
- The timing jitter is a result of ASE noise addition to the signal.
- No Gordon-Haus effect since $\langle \beta_2 \rangle = 0$.



ASE noise jitter

■ RESULTS FROM PTDS SIMULATION (TOTAL DISTANCE EQUAL TO 1800 KM):

- Without adding ASE noise to the signal:



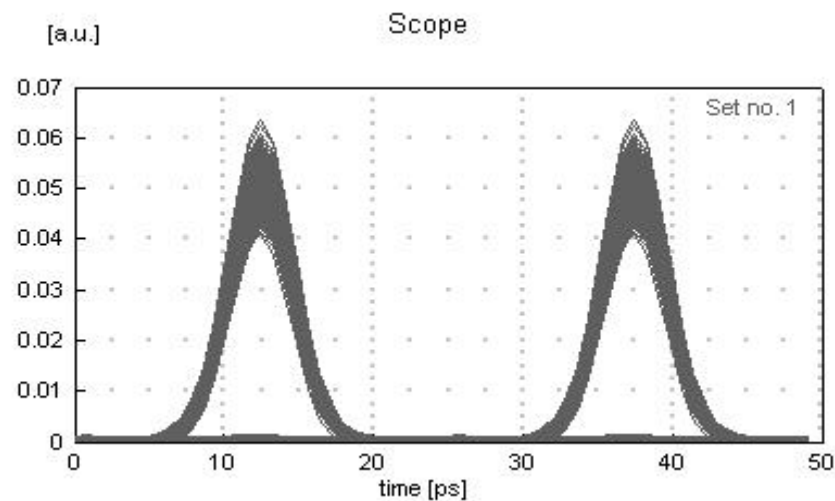
- No timing jitter appear. Thus the source must be the ASE noise.



ASE noise jitter

■ RESULTS FROM PTDS SIMULATION:

- Attenuator + amplifier:



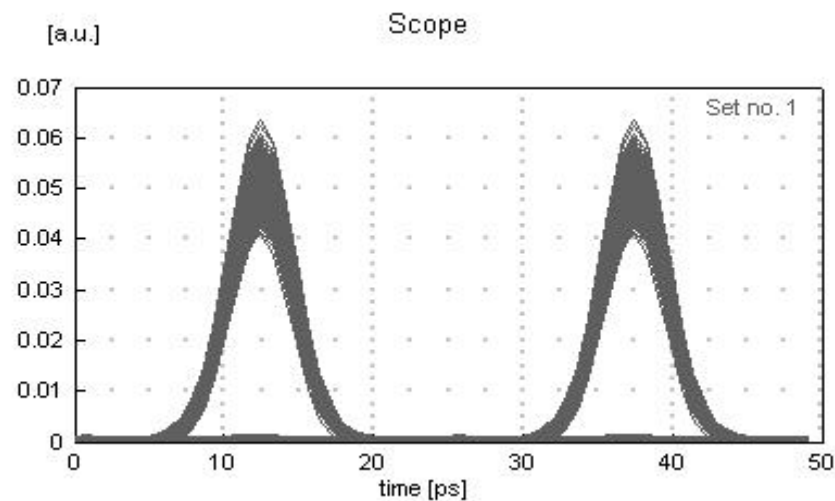
- Timing jitter is equal to 0.14 (ps).



ASE noise jitter

■ RESULTS FROM PTDS SIMULATION:

- Dispersion poscompensation with fiber grating:



- Timing jitter is equal to 0.14 (ps).
- The similar results between the two last configurations, allows to conclude that there is not Gordon-Haus effect in such a system.



ASE noise jitter

- Following the work done by [Georges93] we have for the pulse jitter at the output of the optical amplifier:

$$\sigma_t^2 = \frac{\pi^2 n_{sp} (G - 1) T_0^2}{6 A_0 N_g}$$

- where N_g is the number of photons by gaussian pulse:

$$N_g = \frac{\text{Gaussian pulse energy}}{\text{Photon energy}} = \frac{2\sqrt{\pi^3} P_0 T_0}{hf}$$

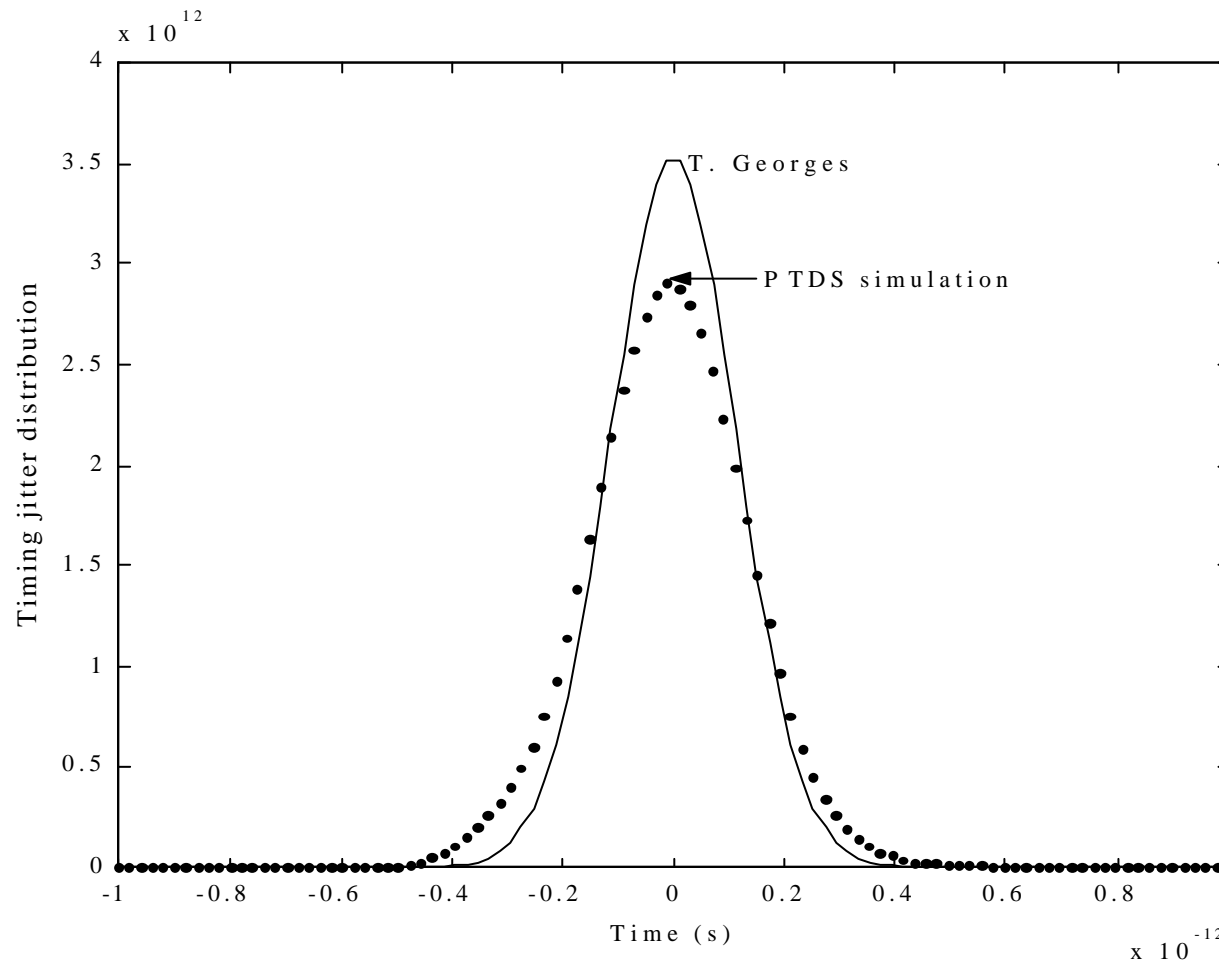
- Results to the timing jitter variance:

$$\sigma_t^2 = \frac{\sqrt{\pi} n_{sp} (G - 1) hf T_0}{12 P_0}$$



ASE noise jitter

■ COMPARISON BETWEEN ANALYTICAL MODEL AND SIMULATION:




$$\sigma_{\text{George}} = 0.11 \text{ (ps)}$$

$$\sigma_{\text{sim}} = 0.14 \text{ (ps)}$$



Conclusions

- The major limiting factors at 40 Gbit/s are:
 - Dispersion
 - Non-linear interaction between pulses
- ASE noise jitter is negligible.
- Total dispersion compensation  No Gordon-Haus effect
- The source of ASE noise jitter is the time fluctuations at the optical amplifier.
- Fiber Bragg grating as dispersion compensation device
- Pre-chirp is a suitable technique to decrease the non-linear interaction

